In this talk we present several Laplace inversion formula. Based on these formula, fast numerical schemes have been developed and used to solving many application problems. We apply and analyze those methods to solve some integro-differential equations and backward parabolic problems. We will also give some comparative remarks on other numerical schemes.