Recent Progress on Wilson Nonconforming Finite Element

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Wilson nonconforming finite element (1973) is a very useful rectangular element In practice. it has been shown in many engineering applications that the convergence behavior of this element is better than that of the commonly used bilinear element. However, mathematical studies carried out so far cannot justify it. The results obtained by use of standard finite element analysis are not satisfactory.

Recently (2007–) we tackle this problem from a different view point, i.e. from Mechanics, where the Wilson element was originated. We have succeeded in proving both mathematically and numerically that the Wilson element is free of shear locking for a wide class of bending dominated plane elasticity problems, while the bilinear element suffers from the shear locking.

Therefore, we elucidate a long-standing folklore: why Wilson element does a better job in many practical applications than the bilinear element.