Inverse of Ill-Conditioned Band Triangular Toeplitz Matrices

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In this talk, we discuss the inverse of ill-conditioned triangular Toeplitz matrices $T_n[p_t]$ generated by

$$p_t(\theta) = \prod_{j=1}^{s} (1 - e^{i(\theta - \theta_j)})^{\mu_j}, \quad -\pi \le \theta \le \pi,$$

where $\mu_j > 0$, j = 1, ..., s are integers. We will give a formula for the enties of $(T_n[p_t])^{-1}$. Based on the formula, we discuss the condition number of $T_n[p_t]$ and address some theoretical problems in the paper "F. R. Lin and W. K. Ching, *Inverse Toeplitz preconditioners for Hermitian Toeplitz systems*, Numerical Linear Algebra with Applications, 12 (2005), pp. 221–229.".

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